## POLYTECHNIC, B.E/B.TECH, M.E/M.TECH, MBA, MCA & SCHOOL

Notes
Syllabus
Question Papers
Results and Many more...

Available @

www.binils.com

	54 Cost
	Reg. No. :
	Question Paper Code: 90822
	B.E./B.Tech. DEGREE EXAMINATIONS, NOVEMBER/DECEMBER 2022.
	Fifth Semester
	Computer Science and Engineering
	MA 8551 — ALGEBRA AND NUMBER THEORY
	(Common to Computer and Communication Engineering/Information Technology)
	(Regulations 2017)
	Time: Three hours Maximum: 100 marks
	PART A — $(10 \times 2 = 20 \text{ marks})$
1	Which of the following set is/are group under (+, .)  (i) Set of all real numbers (ℝ)  (ii) N - set of natural number
	<ul><li>(ii) N - set of natural number</li><li>(iii) Set of all integer (z)</li></ul>
	(iv) All of the above
	(b) True (or) False: Every subgroup of a cyclic group is cyclic.
	<ul><li>2. If R has no proper divisors of zero. Then R is called ————</li><li>(a) Field (b) integral domain</li></ul>
	(a) Field (b) integral domain (c) group (d) none of these
	3. Define Root of polynomial.
	4. Define relatively prime.
	<ol> <li>Find the number of positive ≤ 2076 and divisible by neither 4 nor 5.</li> </ol>

## POLYTECHNIC, B.E/B.TECH, M.E/M.TECH, MBA, MCA & SCHOOL

Notes
Syllabus
Question Papers
Results and Many more...

Available @

www.binils.com

- 6. Express 10110<sub>two</sub> in base ten.
- 7. Prove that no prime of the form 4n+3 can be expressed as the sum of two squares.
- 8. Solve the linear system  $x \equiv 1 \pmod{3}$ ,  $x \equiv 2 \pmod{4}$ ,  $x \equiv 3 \pmod{5}$ .
- 9. Statement only: Fermat's little theorem.
- 10. Define Euler phi function.

PART B — 
$$(5 \times 16 = 80 \text{ marks})$$

- 11. (a) For every group G, prove that the following statements.
  - (i) the identity of G is unique.
  - (ii) the inverse of each element of G is unique.
  - (iii) if  $a,b,c \in G$  and ab = ac then b = c. (Left cancellation property)
  - (iv) if  $a,b,c \in G$  and ba = ca, then b = c. (Right cancellation property) (16)

(b) (i) State and prove the Lagrange's theorem.
(8)
(ii) Given a ring (R,+,.) for all a, b∈ R, prove that the following

Or

(1) -(-a) = a,

statements

- (2) a(-b) = (-a)b = -(ab), and
- (3) (-a)(-b) = ab

(8)

- 12. (a) (i) If  $f(x) = 3x^2 + 4x + 2$  and  $g(x) = 6x^4 + 4x^3 + 5x^2 + 3x + 1$  are polynomial in  $\mathbb{Z}_7[x]$ , Find finite field. (8)
  - (ii) If  $f(x) \in F[x]$  has degree  $n \ge 1$ , then prove that f(x) has at most n roots in F.

Or

- (b) (i) Prove that a finite field F has order  $p^t$ , where p is prime and  $t \in \mathbb{Z}^+$ 
  - (ii) Let (F,+,.) Be a field. If char(F) > 0, then prove that the char(F) must be prime.

90822

## POLYTECHNIC, B.E/B.TECH, M.E/M.TECH, MBA, MCA & SCHOOL

Notes Syllabus Question Papers Results and Many more... Available @

www.binils.com

