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Question Paper Code: 41307

B.E./B.Tech. DEGREE EXAMINATION, APRIL/MAY 2018

Second Semester

Mechanical Engineering MA 6251 – MATHEMATICS – II

(Common to Mechanical Engineering (Sandwich)/Aeronautical Engineering/ Agriculture Engineering/Automobile Engineering/Biomedical Engineering/ Civil Engineering/Computer Science and Engineering/Computer and Communication Engineering/Electrical and Electronics Engineering/Electronics and Communication Engineering /Electronics and Instrumentation Engineering/

Environmental Engineering/Geoinformatics Engineering/Industrial Engineering/
Industrial Engineering and Management/Instrumentation and Control
Engineering/Manufacturing Engineering/Materials Science and Engineering/
Mechanical and Automation Engineering/Mechatronics Engineering/Medical
Electronics/Petrochemical Engineering/Production Engineering/Robotics and
Automation Engineering/(Common to all Branches except Marine Engg.)/Bio
Technology/Chemical Engineering/Chemical and Electrochemical Engineering/
Fashion Technology/Food Technology/Handloom and Textile Technology/
Information Technology/Petrochemical Technology/Petroleum Engineering/
Pharmaceutical Technology/Plastic Technology/Polymer Technology/Textile

Pharmaceutical Technology/Plastic Technology/Polymer Technology/Textile Chemistry/Textile Technology/Textile Technology (Fashion Technology)
(Regulations 2013)

Time: Three Hours

Maximum: 100 Marks

Answer ALL questions.

PART - A

(10×2=20 Marks)

- 1. In what direction from (-1, 1, 2) is the directional derivative of $\phi = xy^2z^3$ a maximum?
- 2. Find the value of 'a' for the vector $\vec{F} = (2x^2y + yz)\vec{i} + (xy^2 xz^2)\vec{j} + (axyz 2x^2y^2)\vec{k}$ to be solenoidal.
- 3. Find the complementary function $\frac{d^3y}{dx^3} 3\frac{d^2y}{dx^2} + 4\frac{dy}{dx} 2y = 0 \ .$
- 4. Write the general form of Cauchy's homogeneous linear equation.

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5. If
$$f(t) = \begin{bmatrix} 3, 0 < t < 2 \\ -1, 2 < t < 4 \\ 0, t \ge 4 \end{bmatrix}$$
, find $L[f(t)]$

- 6. State and prove change of scale property.
- 7. Verify whether $w = (x^2 y^2 2xy) + ix^2 y^2 + 2xy$ is an analytic function of z = x + iy.
- 8. Define conformal mapping.
- 9. Evaluate $\int_C (z^2 z + 1) dz$ where C is the circle |z| = 2.
- 10. Write the Laurent's series expansion.

PART - B

(5×16=80 Marks

11. a) i) Prove that div grad $r^n = n(n+1)r^{n-2}$.

(8)

- ii) Find the work done in moving a particle in the force field $\vec{F} = 3x^2 \vec{i} + (2xz y) \vec{j} + z \vec{k}$ along the straight line from (0, 0, 0) to (2, 1, 3). (8)
- b) i) Evaluate $\oint [xy + x^2] dx + [x^2 + y^2] dy$ where c is the square formed by the lines x = 1, x = -1, y = 1, y = -1 using Green's theorem in the plane. (6)
- ii) Verify Stoke's theorem for $\vec{F} = y^2 \vec{i} + y \vec{j} xz \vec{k}$ over the upper half of the sphere $x^2 + y^2 + z^2 = a^2$, $z \ge 0$. (10)
- 12. a) i) Solve: $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = \log x \sin(\log x)$. (8)
 - ii) Solve by the method of variation of parameters $\frac{d^2y}{dx^2} 3\frac{dy}{dx} + 2y = \frac{e^x}{1 + e^x}$. (8)
 - b) i) Solve $(3x+2)^2 \frac{d^2y}{dx^2} + 3(3x+2)\frac{dy}{dx} 36y = 3x^2 + 4x + 1.$ (8)
 - ii) Solve the system of equations $\frac{dx}{dt} + 2y = -\sin t$; $\frac{dy}{dt} 2x = \cos t$. (8)

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